

Influence of epitaxial strain on the ferromagnetic semiconductor EuO: First-principles calculations

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(Received 29 November 2007; revised manuscript received 23 December 2007; published 7 March 2008)

From first-principles calculations we investigate the electronic structure and the magnetic properties of EuO under hydrostatic stress and the appropriate biaxial stress for epitaxial films. There is a complex interdependence of the O $2p$ and Eu $4f$ and $5d$ bands on the magnetism in EuO, and decreasing lattice parameters is an ideal method to increase the Curie temperature T_c . Compared to hydrostatic pressure, the out-of-plane compensation that is available to epitaxial films diminishes this increase in T_c , although the T_c increase is nonetheless significant due to the small value of Poisson's ratio for EuO. We find the semiconducting gap closes at a 6% in-plane lattice compression for epitaxy, at which point a significant conceptual change must occur in the active exchange mechanisms.

DOI: [10.1103/PhysRevB.77.121202](https://doi.org/10.1103/PhysRevB.77.121202)

PACS number(s): 75.70.Ak, 62.20.dj, 62.50.-p, 71.15.Mb

The desire to connect the electronic and magnetic properties of materials to enable new device characteristics has renewed focus on the many unique properties of EuO, one of the initially discovered ferromagnetic semiconductors.¹ The divalent Eu ions in EuO possess a very large local moment from the half filled $4f$ band producing a saturation magnetization of $7\mu_B$,^{1,2} while a gap of 1.2 eV separates the half filled $4f$ band from the $5d6s$ conduction band.³ Low levels of electron doping are readily achieved with oxygen vacancies EuO_{1-x} , leading to an insulator-to-metal transition (IMT) in conjunction with the ferromagnetic ordering⁴ and 100% spin polarization of the conduction electrons.⁵ EuO may therefore be a good candidate for a spin injection material. Cation and anion doping has been shown to increase the Curie temperature (T_c) up to 170 K,⁶⁻⁸ from that of 69 K for stoichiometric EuO.²

The integration of EuO_{1-x} with Si and GaN has been successfully demonstrated^{8,9} so there is renewed interest in increasing T_c towards room temperature to enable spintronic applications. Beyond the effects of doping on T_c , it has been shown that a hydrostatic pressure of about 100 kbar can increase T_c to 200 K.¹⁰ Although hydrostatic pressure is not an option for device applications, a similar effect on T_c may be obtainable by using epitaxial strain. However, epitaxy generates a biaxial stress state which is quite different from the isotropic stress state of hydrostatic pressure. Furthermore, there are a number of competing exchange mechanisms that determine the magnetism in EuO, and it is not known exactly how this competition plays out as the lattice parameters are changed.

In this Rapid Communication we explore the effects of biaxial stress in comparison with isotropic stress on the band structure and magnetism of EuO with density functional theory (DFT). We find that the biaxial stress state expected in an epitaxial film will lead to a 50% increase in the T_c before an insulator-to-metal transition occurs. This increase, although not as great as that found for isotropic stress, is much larger than expected for a three-dimensional material under biaxial stress due to the small value of Poisson's ratio for EuO. From a band structure perspective of the magnetism in EuO, we find that reducing lattice parameters is an ideal

method of increasing T_c . Although the closing of the semiconducting gap, which we find at 5% compression for isotropic stress and 6% compression of biaxial stress, must lead to a conceptually different exchange mechanism, no sudden changes are seen in the magnetic properties. The combined effects of doping and epitaxy are explored and are found to generate a significant increase in the mean field T_c of up to 175 K.

The EuO band structure is calculated with the full-potential linearized augmented plane-wave DFT code WIEN2K.¹¹ The exchange and correlation effects are treated within the generalized gradient approximation (GGA), after Perdew *et al.*¹² The LSDA+ U method¹³ was used to account for strong correlations between the electrons in the Eu $4f$ shell. Note that standard GGA or local spin density approximation (LSDA) predict EuO to be a metal whereas measurements clearly show the existence of conductivity gap.³ The exchange parameter ($J_H=0.77$ eV) was chosen according to Ref. 14, and the on-site Coulomb repulsion for the Eu $4f$ orbital was set to $U_f=8.3$ eV, while those of the O p orbital were $U_p=4.6$ eV and $J_H=1.2$ eV.¹⁵⁻¹⁷ With these values the LSDA+ U band structure with the {001} antiferromagnetic spin configuration (AFM_I) or the NiO-type {111} AFM spin configuration (AFM_{II}) shows a gap of 1.2 and 1.3 eV, respectively. The ferromagnetic (FM) spin arrangement exhibits a gap of 0.7 eV (see Fig. 1). Both are consistent with the experimental optical absorption gaps of 0.9 and 1.2 eV observed below and above the magnetic transition temperature.^{18,19} Our calculations show a minimum in the total energy of the bulk EuO at $a=5.1578$ Å, in good agreement with the measured lattice parameter of 5.1439 Å.²⁰ All calculations were done with fixed muffin-tin radii and with 420 k points in the Brillouin zone of a supercell compatible with all three magnetic spin configurations so as to minimize sources of numerical errors.

The calculations were done for the isotropic stress case of hydrostatic pressure, where the cubic unit cell is maintained, and the biaxial stress case of epitaxial film growth where the unit cell becomes tetragonal. For all the biaxial stress case calculations, the in-plane lattice parameter is held fixed and the minimum in the total energy is found as a function of the c lattice parameter.

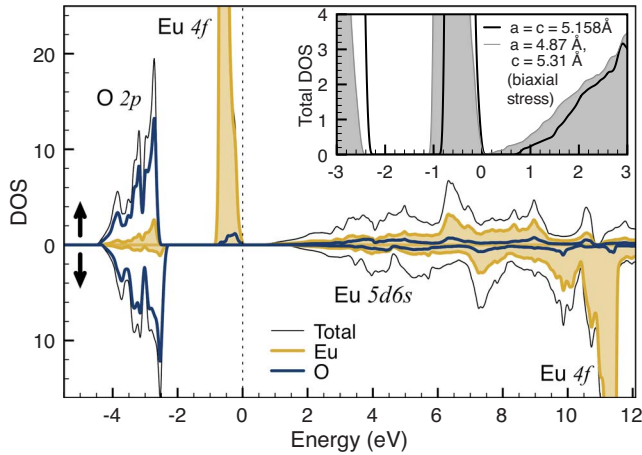


FIG. 1. (Color online) The spin resolved density of states of bulk EuO in the FM configuration with optimized bulk lattice parameters, $a=5.1578$ Å. The bands are labeled and the zero of energy is at the Fermi energy E_f . The inset shows the total density of states of the bulk ($a=c=a_0=5.158$ Å) and the biaxial stress case just prior to the IMT ($a=4.87$ Å, $c=5.31$ Å).

Since the Eu 2+ ion is in the f^7 high spin configuration, the magnetic properties of EuO are often described by a Heisenberg model. According to the description of Mauger and Godart,³ the nearest neighbor exchange J_1 is based on a 4f electron having a virtual excitation to the 5d band where it experiences an exchange interaction with the 4f spin on a nearest neighbor. This leads to ferromagnetic coupling. The nature of the next-nearest neighbor exchange constant J_2 is thought to be rather complex and involves various competing exchange paths between the O 2p, Eu 5d, and 4f orbitals. A model calculation of J_2 in EuO shows that it is still ferromagnetic, but only about 30% the size of J_1 .³

In the isotropic stress case, we can extract J_1 and J_2 coupling constants from our calculations by relating the total energies of the various magnetic configurations (FM, AFM_I, AFM_{II})²¹ from the LSDA calculations with the Heisenberg model. We assume that the third nearest neighbor coupling J_3 is very small.^{22,23} From these values, shown as a function of lattice parameter in Fig. 2(a), we can calculate a mean field value for $T_c=(2/3)S(S+1)(12J_1+6J_2)$. Our exchange parameters for the optimized bulk lattice parameter ($J_1=0.66$ K, $J_2=0.19$ K) are in good agreement with neutron measurements, and previous calculations.^{23,24}

Previous experimental studies have looked at the effect of hydrostatic pressure on T_c (Refs. 10 and 25) and the unit cell volume²⁶ in EuO. In Fig. 2(b) we combine that data to plot the experimental change in T_c as a function of lattice parameter. Included in this figure is our calculation of the mean field T_c of the isotropic case as the lattice parameter is changed. There is quite good agreement between the experimental and calculated mean field T_c , with the expected overestimation of the mean field value.

The calculations for the isotropic stress case indicate the closing of the Eu 4f-Eu 5d6s gap, or IMT, at $a/a_0=0.95$. This compares well with the appearance of a drude-like peak in the optical reflectivity and a jump in the room temperature resistivity at a pressure of ≈ 130 kbar, or $a/a_0=0.96$.^{10,26} As

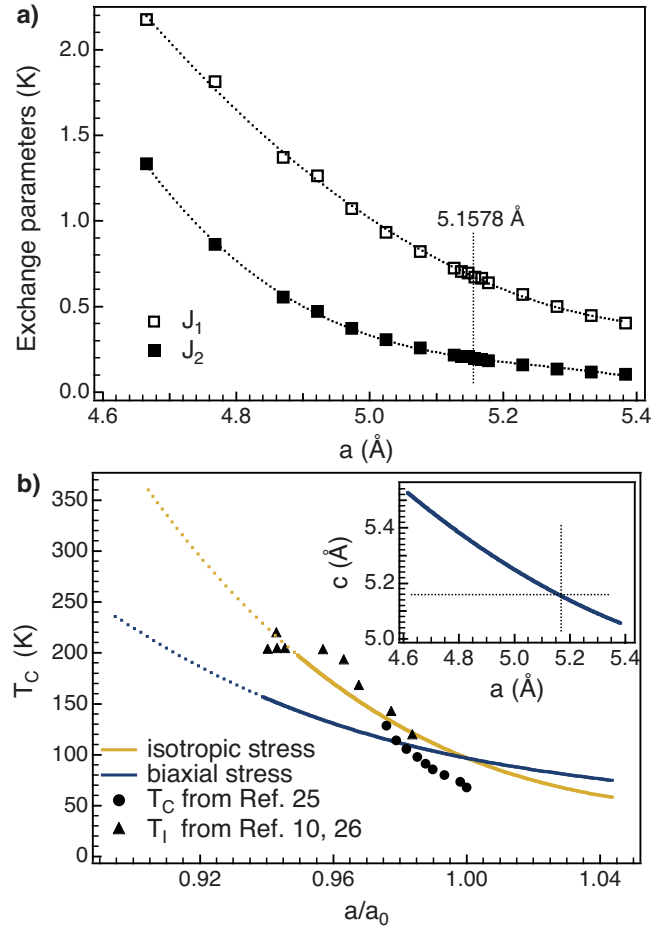


FIG. 2. (Color online) (a) The nearest neighbor and next-nearest neighbor exchange constants J_1 and J_2 as a function of the normalized in-plane lattice parameter for the isotropic stress case. (b) The calculated mean field T_c as a function of in-plane lattice parameter for the isotropic stress case and the biaxial stress state of an epitaxial film. Both solid lines change to dashed lines at their respective IMT. Included in the graph is the experimental T_c , from susceptibility measurements, of Ref. 25 (circles), and T_I —which tracks T_c (Ref. 10)—determined via resistivity measurements in Ref. 10 in combination with the pressure-volume relations from Ref. 26 (triangles). The inset shows the change in the out-of-plane lattice parameters in the biaxial stress case.

seen in Fig. 2(b), a saturation of the experimental parameter T_I ,¹⁰ which is thought to track T_c , is also found around $a/a_0=0.96$. If T_I does in fact track T_c , then this saturation may be connected to the filled spin-up 4f and empty 5d bands starting to overlap. This would generate a mixed configuration of the $J=7/2$ magnetic Eu 4f⁷ configuration and the $J=0$ nonmagnetic Eu 4f⁶ configuration.²⁶ Within our calculations for EuO with lattice parameters smaller than the IMT values, a $J=7/2$ magnetic configuration is always generated as the real many-body nature of the $J=0$ singlet state is not accessible from the LDA framework. Therefore, our calculations do not include the possible disruption of the magnetic order from the f^6 configuration and we find T_c continuing to rapidly rise after the gap has closed. As the material becomes more metallic with increasing doping, other exchange mechanisms such as RKKY would start play-

ing an increasingly important role. The transition, however, will be smooth as the Fermi wave vector k_f in the metallic state will be very small due to the low doping level.

The mean field T_c for the biaxial stress case is also included in Fig. 2(b). This is calculated as $T_c = (2/3)S(S+1)[(4J_1^{\parallel} + 8J_1^{\perp}) + (4J_2^{\parallel} + 2J_2^{\perp})]$. The in-plane (\parallel) and out-of-plane (\perp) nearest and next-nearest neighbor distances are calculated from the optimized FM tetragonal structure at a given a lattice parameter, and the appropriate J_1 and J_2 exchange parameter values are determined for these distances from the data presented in Fig. 2(a). The biaxial stress shows a smaller effect on T_c for a given in-plane lattice parameter change as compared to the isotropic stress case. This occurs because the average atomic distances change more slowly in the biaxial stress state due to the ability of the out-of-plane lattice spacing to compensate for changes in the in-plane lattice parameter. The IMT is now found to occur at $a/a_0=0.94$. As in the isotropic stress calculation, we find T_c continuing to increase as lattice parameters are decreased beyond the IMT. The inset of Fig. 1 shows the total density of states of the biaxial stress case when the IMT occurs.

The compensation for the in-plane lattice parameter change in the biaxial stress case is shown in the inset of Fig. 2(b). The relationship between the in-plane a , and out-of-plane c lattice parameters for the biaxial stress state is given by $\frac{\Delta a}{a} = \frac{-2\nu \Delta c}{1-\nu c}$, where ν is Poisson's ratio. ν is calculated to be 0.15. This is very close to the experimental value of 0.2 for NiO,²⁷ and the calculated value of 0.2 for GdN.²²

Magnetism in EuO is related to three main types of exchange mechanisms: local, or on-site exchange between the Eu 4*f* and other Eu orbitals; a Kramers-Anderson superexchange;²⁸ and a number of other virtual exchange possibilities across the semiconducting gap. The on-site exchange between Eu 4*f* and 5*d* is large, but cannot, by itself, generate long range FM order. However, it plays a major role in the various virtual exchange mechanisms. The Kramers-Anderson superexchange, a conceptually important exchange mechanism, originates from the overlap of Eu 4*f* and O 2*p* orbitals. However, since the O 2*p*-Eu 4*f* hopping parameters are quite small, when compared to O 2*p*-3*d* hopping in transition metal oxides, this antiferromagnetic component of J_2 plays only a minor role in EuO. If the gap between the O 2*p*-Eu 4*f* states were to drastically reduce, increasing the overlap in energy of the states, this mechanism would become much more pronounced. Nonetheless, this can only be achieved by changing the chemistry of the europium chalcogenides; lattice parameter changes are not enough. Although the exact decomposition of all possible virtual exchange mechanisms due to the excitations across the semiconducting gap is outside the scope of this work, by using a constrained potential in LSDA, one can change the energy of a specific orbital and effectively control the hopping integrals associated with that orbital. This helps to separate out what types of changes in the band structure are most significant to the ferromagnetism.

We find that in order to most effectively increase T_c , the hybridization between Eu 4*f* and 5*d* should be increased, as should that of the O 2*p* and Eu 5*d* bands, while at the same time minimizing the O 2*p* to Eu 4*f* hybridization. Since the

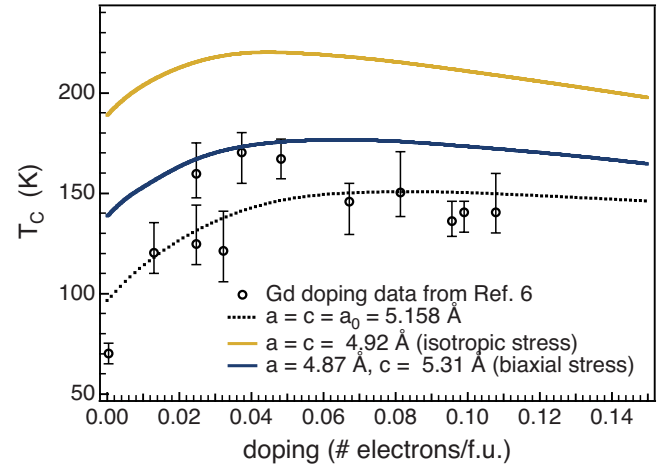


FIG. 3. (Color online) The mean field T_c as a function of electron doping for bulk ($a=c=a_0=5.158$ Å), isotropic stress ($a=c=4.92$ Å), and biaxial stress ($a=4.87$ Å, $c=5.31$ Å). T_c of Gd doping from Ref. 6.

Eu 4*f* band sits between the O 2*p* and the Eu 5*d* in EuO it is not possible to do all three at the same time. However, the gap between the Eu 4*f* and 5*d* bands closes much more rapidly than the O 2*p* and Eu 4*f* band gap, so there is minimal loss in the ferromagnetic exchange due to the O 2*p*-Eu 4*f* superexchange from decreasing lattice parameters. Therefore, we find that decreasing lattice parameters in EuO is an ideal way of strengthening the ferromagnetic exchange.

Finally, by looking at the total energy changes due to a rigid band shift of the chemical potential for the FM, AFM_I, and AFM_{II} configurations, we can also study the combined effect of isotropic or biaxial stress and electron doping on the mean field T_c . Figure 3 shows these results for three situations; bulk lattice parameters, an isotropic stress case on the insulating side of the IMT ($a/a_0=0.955$), and a biaxial stress case on the insulating side of the IMT ($a/a_0=0.945$). At low doping, T_c immediately increases in all cases because of the gain in total energy of the FM configuration relative to either of the AFM configurations. As doping increases, the energy cost to add extra electrons into both FM and AFM configurations becomes similar and a maximum in T_c is reached. Our calculations suggest that the density of states of a 5.5% biaxially compressed epitaxial film would allow a significant increase in T_c , from 138 to 175 K.

Also included in Fig. 3, for comparison, are data from Gd doping experiments of Ott *et al.*⁶ In essence, Gd doping is adding one electron per Gd atom to EuO while leaving the $S=7/2$ spin configuration unchanged. The maximum change in T_c with Gd doping is about twice the size expected for electron doping via a rigid band shift of the chemical potential. This suggests that there are some further effects present. One possibility is that subtle changes occur in the 5*d*_{6*s*} bands which affect the 4*f* to 5*d* exchange. The presence of the smaller Gd³⁺ ion may also provide a positive chemical pressure on the EuO matrix and decrease lattice parameters, activating all the previously discussed mechanisms. It is worth noting that if the impressive T_c enhancement from Gd

is related to chemical pressure, then Gd would be a less effective means of increasing the T_c of a film that is already biaxially compressed.

In conclusion, we find that the strain from epitaxy can be used to increase the T_c of EuO. However, we show that the effect of the biaxial stress generated by epitaxy is not as effective as hydrostatic pressure due to the ability of the out-of-plane lattice parameter to partially compensate for the in-plane lattice changes. The amount of out-of-plane compensation is minimized for the three-dimensional isotropic rocksalt-type structure in EuO because of its small Poisson ratio. A material with a two-dimensional electronic structure would allow for the ultimate minimization of the out-of-plane compensation inherent in the biaxial stress state of epitaxy, although the likelihood of buckling or other structural modifications would be enhanced. From the band structure

perspective we find that the location of the near E_f bands suggests that a decrease in lattice parameters is an ideal means of increasing T_c , as it strongly enhances the main ferromagnetic exchange mechanisms. The closing of the semiconductor gap is found to occur at a 5% lattice reduction in the isotropic stress case, or 6% reduction in the biaxial stress state. Although the closing of the gap will change the next-nearest neighbor exchange mechanism, there is no sudden change in the magnetic properties. Finally, we find that electron doping will lead to an increase in T_c for isotropically and biaxially compressed films.

We gratefully acknowledge George Sawatzky for enlightening discussions. This work was supported by the Natural Sciences and Engineering Research Council of Canada and enabled by the use of WestGrid computing resources.

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